

## SURFACE AREA - ANSWERS

Use the formula  $\text{Surface Area} = \iint_S dS = \iint_R \sqrt{\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 + 1} dA$  to find the surface area of the following planes over the region defined, for problems 1 through 3, by the intervals  $0 \leq x \leq 1$  and  $0 \leq y \leq 1$ , and, for problems 4 and 5, by the intervals  $0 \leq x \leq 2$  and  $0 \leq y \leq 2$ .

1.  $z = x + y + 3$

$$\iint_S dS = \iint_R \sqrt{\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 + 1} dA = \int_0^1 \int_0^1 \sqrt{1+1+1} dydx = \sqrt{3}$$

2.  $z = 2x - y + 1$

$$\iint_S dS = \iint_R \sqrt{\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 + 1} dA = \int_0^1 \int_0^1 \sqrt{4+1+1} dydx = \sqrt{6}$$

3.  $z = 3x + 2y + 4$

$$\iint_S dS = \iint_R \sqrt{\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 + 1} dA = \int_0^1 \int_0^1 \sqrt{9+4+1} dydx = \sqrt{14}$$

4.  $z = 8x + 4y + 2$

$$\iint_S dS = \iint_R \sqrt{\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 + 1} dA = \int_0^2 \int_0^2 \sqrt{64+16+1} dydx = 4\sqrt{81} = 36$$

5.  $z = -x - y - 10$

$$\iint_S dS = \iint_R \sqrt{\left(\frac{\partial z}{\partial x}\right)^2 + \left(\frac{\partial z}{\partial y}\right)^2 + 1} dA = \int_0^2 \int_0^2 \sqrt{1+1+1} dydx = 4\sqrt{3}$$