SPHERICAL INTEGRALS

For each problem below, set up and evaluate a triple integral in spherical coordinates.

- 1. Let V be a sphere with center at the origin and radius = r. Find the volume of V.
- 2. Find the volume of the solid bounded by the sphere $x^2 + y^2 + z^2 = 1$ and the cone $z = \sqrt{x^2 + y^2}$.
- 3. Evaluate $\iiint_V \frac{1}{x^2 + y^2 + z^2} dV$ where *V* is the solid region between the spheres $x^2 + y^2 + z^2 = 4$ and $x^2 + y^2 + z^2 = 9$.
- 4. Find the volume of the solid bounded above by z = 1 and below by $z = \sqrt{x^2 + y^2}$.
- 5. Find the volume of the solid region defined by $\rho = \sin \varphi$ where $0 \le \theta \le 2\pi$ and $0 \le \varphi \le \pi$.