## SPHERICAL INTEGRALS

For each problem below, set up and evaluate a triple integral in spherical coordinates.

1. Let $V$ be a sphere with center at the origin and radius $=r$. Find the volume of $V$.
2. Find the volume of the solid bounded by the sphere $x^{2}+y^{2}+z^{2}=1$ and the cone $z=\sqrt{x^{2}+y^{2}}$.
3. Evaluate $\iiint_{V} \frac{1}{x^{2}+y^{2}+z^{2}} d V$ where $V$ is the solid region between the spheres $x^{2}+y^{2}+z^{2}=4$ and $x^{2}+y^{2}+z^{2}=9$.
4. Find the volume of the solid bounded above by $z=1$ and below by $z=\sqrt{x^{2}+y^{2}}$.
5. Find the volume of the solid region defined by $\rho=\sin \varphi$ where $0 \leq \theta \leq 2 \pi$ and $0 \leq \varphi \leq \pi$.
