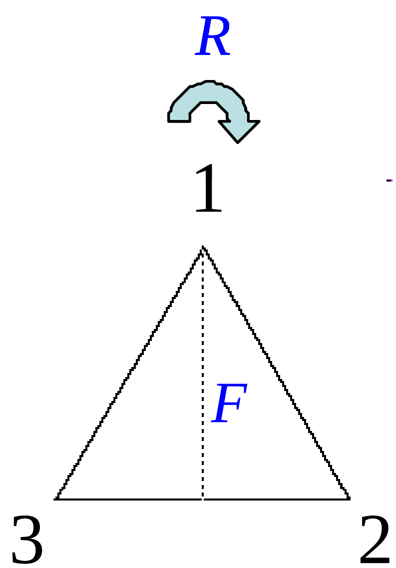
PRACTICE – SUBGROUPS

1. The group of symmetries of the equalateral triangle, S_3, has six subgroups, one of which is the trivial subgroup $\{e\}$ and another is the whole group itself. Use the multiplication table below to find the remaining four subgroups.

	$(1)(2)(3)$	$(1\ 2)$	$(1\ 3)$	$(2\ 3)$	$(1\ 2\ 3)$	$(1\ 3\ 2)$
$(1)(2)(3)$	$(1)(2)(3)$	$(1\ 2)$	$(1\ 3)$	$(2\ 3)$	$(1\ 2\ 3)$	$(1\ 3\ 2)$
$(1\ 2)$	$(1\ 2)$	$(1)(2)(3)$	$(1\ 2\ 3)$	$(1\ 3\ 2)$	$(1\ 3)$	$(2\ 3)$
$(1\ 3)$	$(1\ 3)$	$(1\ 3\ 2)$	$(1)(2)(3)$	$(1\ 2\ 3)$	$(2\ 3)$	$(1\ 2)$
$(2\ 3)$	$(2\ 3)$	$(1\ 2\ 3)$	$(1\ 3\ 2)$	$(1)(2)(3)$	$(1\ 2)$	$(1\ 3)$
$(1\ 2\ 3)$	$(1\ 2\ 3)$	$(2\ 3)$	$(1\ 2)$	$(1\ 3)$	$(1\ 3\ 2)$	$(1)(2)(3)$
$(1\ 3\ 2)$	$(1\ 3\ 2)$	$(1\ 3)$	$(2\ 3)$	$(1\ 2)$	$(1)(2)(3)$	$(1\ 2\ 3)$



2. For each subgroup of order 2 or 3 in S_3, find the left coset created by multiplying the subgroup on the left by the permutation $(1\ 2\ 3)$.

3. Prove: S_3 has no subgroup of order 5.

4. Prove: For any group G, $\{e\}$ is a normal subgroup.